Roll No.					Total No. of Pages : 3

Total No. of Questions : 09

B.Tech. (Sem.-2<sup>nd</sup>)

# ENGINEERING MATHEMATICS-II Subject Code : BTAM-102 (2011 Batch) Paper ID : [A1111]

Time: 3 Hrs.

Max. Marks : 60

## **INSTRUCTION TO CANDIDATES :**

- 1. SECTION-A is COMPULSORY consisting of TEN questions carrying TWO marks each.
- 2. SECTION B & C. have FOUR questions each.
- 3. Attempt any FIVE questions from SECTION B & C carrying EIGHT marks each.
- 4. Select atleast TWO questions from SECTION B & C.

### **SECTION-A**

- l. Solve the following sums :
  - (a) Test whether the set of vectors {(1,1,1), (1,-1,1), (3,-1,3)} are LI or LD by giving suitable reason ?

(b) Find the rank of the matrix 
$$\begin{pmatrix} 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 3 & 1 & 0 & 2 \\ 1 & 1 & -2 & 0 \end{pmatrix}$$

(c) Reduce the matrix 
$$\begin{pmatrix} 1 & 0 & -1 \\ 1 & 2 & 1 \\ 2 & 2 & 3 \end{pmatrix}$$
 to diagonal form.

(d) If  $x = \cos\theta + i \sin\theta$ , and  $y = \cos\phi + i \sin\phi$ , then show that

$$\frac{x-y}{x+y} = i \tan \frac{\theta-\phi}{2}$$

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(e) Find all the values of 
$$\left(\frac{1}{2} + \frac{\sqrt{3}}{2}i\right)^{3/4}$$

(f) Examine the conditional convergence of the series  $\sum_{n=1}^{\infty} \frac{(-1)^{n-1}}{2n-1}.$ 

(g) Test the convergence of the series  $\sum_{n=1}^{\infty} \left(1 + \frac{1}{n}\right)^{-n^2}$ .

(h) Show that the necessary condition for the differential equation  $M dx + N dy = 0 \frac{\partial M}{\partial y} = \frac{\partial N}{\partial x} \text{ is}$ 

(i) Find the particular solution of the equation  $\frac{d^3y}{dx^3} + 4\frac{dy}{dx} = \sin 2x$ .

(j) Solve the equation  $e^{2z-1} = 1 + i$ 

#### **SECTION-B**

- 2. (a) Obtain the general solution of the equation  $y'' 6y' + 9y = e^{3x} / x^2$ , by using method of variation of parameters,
  - (b) Find the complete solution of the differential  $y'' 2y' + y = x e^x \sin x$ .
- 3. (a) Solve the following simultaneous differential equation

$$\frac{dx}{dt} - 2y + 5x = t, \ \frac{dy}{dt} + 2x + y = 0.$$
 Given that  $x(0) = 0, \ y(0) = 0.$ 

(b) Find the complete solution of the differential equation

$$(1 + x)^2 y'' + (1 + x)y' + y = 2\sin \log(1 + x).$$

by using operator method.

4. (a) Solve the differential equation  $(xy^2 - e^{1/x^3}) dx - x^2 y dy = 0$ 

(b) Solve the equation  $y = 2px + yp^2$  where p has its usual meaning.

5. An e.m.f.  $E \sin pt$  is applied at t = 0 to a circuit containing a capacitance C and inductance L. The current *i* satisfies the equation  $L \frac{di}{dt} + \frac{1}{C} \int i dt = E \sin pt$ . If  $p^2 = 1/LC$  and initially the current and the charge are zero then find the current at any time *t*.

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### **SECTION-C**

6. (a) Use the rank method to test the consistency of the system of equations

4x - y = 12; -x + 5y - 2z = 0; -2y + 4z = -8;

if consistent then solve it completely,

(b) State Cayley-Hamilton theorem. Use it to find the inverse of the matrix

$$\begin{pmatrix} 4 & 3 & 1 \\ 2 & 1 & -2 \\ 1 & 2 & 1 \end{pmatrix}$$

7. (a) Find the eigen values and the corresponding eigen vectors of the matrix

$$\begin{pmatrix}
1 & 1 & 3 \\
1 & 5 & 1 \\
3 & 1 & 1
\end{pmatrix}$$

- (b) Prove that eigen values of a skew hermetian matrix are either zero or purely imaginary.
- 8. (a) Test for what values of x the series

$$\sum_{n=1}^{\infty} \frac{\sqrt{n}}{\sqrt{n^2+1}} x^n, x > 0$$

Convergences/diverges

(b) Test convergence/diverge of the series

$$\sum_{n=1}^{\infty} \left[ \sqrt{(n^4+1)} - \sqrt{(n^4-1)} \right]$$

- 9. (a) Use Demoivre's theorem to solve the equation  $(z 1)^5 + z^5 = 0$ 
  - (b) Separate  $\sin^{-1}(e^{i\theta})$  into real and imaginary parts, where  $\theta$  is a positive acute angle.